

Index

- Abelian group, infinite 247–248
- absorption 30–31, 33, 35
- absorption coefficient 30, 32–35, 38
- absorption transitions, induced 12, 35
- actinides 145–146, 167, 171, 180, 182, 185, 192, 194, 196–199, 201, 203–204, 206–209
 - divalent 202, 209
 - tetravalent 145, 192, 197–198, 202, 204, 207, 209
 - trivalent 202, 209
- angular momentum 62–63, 66, 70–71, 73–76, 81–82, 167, 269, 272
- approximation
 - adiabatic 353–354, 357
 - linear 118, 122, 133, 159, 192, 197–198, 203–204, 207
- band gap 178, 389, 395, 397, 401–402, 409–411
- band structure 397–398, 401–403, 411
 - electronic 390, 395–396, 403
- barycenters 127, 164–165, 183–184, 293–294
- basis functions 264–266, 268, 272, 278
- Ce^{3+} 171, 330–331, 333–335, 395, 406, 409–410, 412–414
- Ce^{3+} energy levels 410
- CFPs, *see* crystal field parameters
- Clebsch–Gordan coefficients 76–79
- coordinates
 - electron 290, 292
 - equilibrium 352, 354
 - impurity ion electrons 313
 - mass-weighted 373, 375, 378–379
 - normal vibrational 372–373, 375, 377, 379, 381
 - nuclear 351–352, 354, 357
- Coulomb interaction parameters 185, 203
- Cr^{3+} 3, 91–92, 371
- Cr^{4+} 92, 324, 371
- crystal field 6, 100, 138, 146, 183, 268, 277, 287–289, 297–298, 303–304, 309, 311, 313, 315, 317, 319, 321–322, 330, 334–335, 337, 392, 400
 - strong 304–306
 - tetrahedral 278, 294, 299–302
- crystal field calculations 183, 370
- crystal field effects, microscopic 329, 390–391, 393
- crystal field Hamiltonian 310–312, 316–317, 325, 331, 333, 335–336, 398, 412, 414
- crystal field interactions 298, 337, 412
- crystal field parameters (CFPs) 101, 142, 150, 164, 183, 310–311, 316, 325, 329, 331, 335, 398
- crystal field-split energy levels 396
- crystal field splittings 277, 288, 296, 325, 329, 336, 396, 403–404

- crystal field strength 293–294, 298, 303, 305–307, 390, 392, 394
- crystal field theory 6, 78, 279, 287–288, 290, 292, 294, 296, 298, 300, 302, 304, 306, 308, 310, 312, 314, 316, 318, 320, 322, 324, 326, 328, 330, 332, 334, 336, 338, 390, 396, 398, 403, 410
 - basic postulates of 287–288, 290, 292, 294, 296, 298, 300, 302, 304, 306, 308, 310, 312, 314, 316, 318, 320, 322, 324, 326, 328, 330, 332, 334, 336, 338
- crystal lattice sites 287, 309–312, 412
- crystal lattice vibrations 349, 365
- CSB crystal 371–372
- degeneracy 12, 53, 66, 81, 274–277, 294
- degenerated energy levels 275, 310, 383
- density functional theory (DFT) 390, 409
- DFT, *see* density functional theory
- DFT-based calculations 402–403
- dipole operators 21–22, 58, 282–283, 358
 - electric 57–58, 60, 268, 280–281
- doped crystals 6, 389, 395, 397, 399, 401, 403, 408–409
- ECM, *see* exchange charge model
- eigenfunctions 47–48, 71, 274, 293
- eigenvalues 47–48, 61, 64, 71, 101, 274, 290, 293, 310, 352–354, 376, 378, 380
- eigenvectors 375–376, 378, 381
- Einstein coefficients 10–13, 24, 34, 38
- electromagnetic wave 30, 32
- electron charge 21, 68
- electron configurations
 - conjugate 171, 211
 - core 193–194
 - excited 180, 412
 - half-filled 165
 - identical 138
 - unfilled 100
- electron density 142, 164, 296
- electron density distribution 55–56
- electron orbitals 3, 69, 312
- electron shell
 - filled 3, 44, 94, 165
 - unfilled 101, 146, 150, 287
- electron-vibrational interaction (EVI) 6, 349–350, 352, 354, 356–358, 360, 362, 364–368, 370, 372, 374, 376, 378, 380, 382, 384, 386, 391
- electronic configurations 69, 81, 89, 91, 99, 101, 145, 147, 152, 164, 166–167, 178, 180–181, 183, 185, 187, 189, 191, 193, 195, 197, 199, 201, 203, 205, 207, 318, 392
- electronic energy levels 370, 423
- electronic states 11, 73, 204, 354, 356–358, 360–361, 363–365, 367–368, 382, 391, 409, 414
 - degenerate 383
 - excited 354, 357–358, 361
- electronic subsystem 351, 353
- electrons radial coordinates 142, 147, 150, 183
- electrostatic interaction 72, 89, 312
- electrostatic matrices 91, 325
- electrostatic parameters 101, 122
 - independent 152

- emission 2–3, 6, 9–11, 14–15, 34, 38–39, 43, 59, 175, 177–178, 355–357, 363–366, 395, 412
- emission transitions 10, 12, 14–15, 19, 34–35, 178, 329, 356, 361, 364, 366, 408
- induced 10–11, 13, 33, 35
- spontaneous 12, 34
- energy
 - barycenter 150, 164
 - electromagnetic field 11–12, 34
 - electron excitation 367
 - electronic 354, 367, 383
 - potential 47, 50, 62, 68, 289, 350, 352, 373, 376–377, 379–381, 383–384
 - spin-pairing 305
- energy eigenvalue 351
- energy level schemes 100, 138, 147, 151, 167, 171–174, 176–177, 179–180, 211, 292, 323, 392, 401, 403
- energy levels calculations 329
- energy levels location 87, 171
- energy levels splitting 122, 138, 279, 297, 309, 331, 333, 390
 - degenerated 246, 268
- energy splitting 150, 184
- energy uncertainties 14
- Eu^{2+} 149, 179, 182, 367, 414
- EVI, *see* electron-vibrational interaction
- exchange charge model (ECM) 309, 311, 313, 322, 324–325, 327, 329, 333–334, 336, 392, 394, 396, 412
- exchange Coulomb interaction 183–184
- excited state lifetime 14, 16, 370–371
- excited state parabola 368, 370
- first-principle and semi-empirical models, combination of 390–414
- free ions 43, 91, 138, 150, 211, 309, 337
 - energy level schemes 145
 - energy levels of 101, 147
- full width at half maximum (FWHM) 16, 18, 365, 367
- FWHM, *see* full width at half maximum
- Gaussian function 18
- Gordan coefficients 77–79
- ground state configurations 149, 151, 305
- ground state electron configuration 329
- ground state parabola 368
- group multiplication rule 246–247
- group theory 6, 245–246, 248, 250–252, 254, 256, 258, 260, 262, 264, 266, 268, 270, 272, 274, 276, 278–281, 284, 287, 310, 326
- group theory analysis 279, 328
- Hamiltonian, free ion 147, 151, 167, 183, 208–211, 412
- Hamiltonian parameters 151, 211–213, 216, 219, 222, 225, 228, 231, 234, 237, 240, 414
- hydrogen 6, 43–46, 48, 50, 52, 54, 56, 58, 60, 62, 64–66, 95
- hydrogen atom 2, 45–47, 52–54, 64–65, 67–69, 93, 95, 296, 352
- hydrogenic ratios 152, 163
- impurity ions 6, 91, 246, 267, 287, 289, 292–293, 297–298, 306, 308–313, 315, 317, 329, 334, 349, 355, 365, 370, 382, 389–391, 395–396, 401
 - energy levels 287, 370
- inequivalent electrons 81, 83
- inter-electron interaction 72

- interionic separations 306, 334, 413
- ionization energies 101, 140–142, 150, 166–167
- ions
 - actinide 145–147, 149–150, 166, 175, 179, 181–182
 - Al^{3+} 389–390, 401
 - aluminum 323
 - Ce^{3+} 329–331, 333, 335, 395, 408, 410–412, 414
 - cerium 409
 - Co^{2+} 277–278
 - Cr^{3+} 3, 308, 370–372, 389
 - Cr^{4+} 279, 322–323, 325–328, 369–370
 - crystal lattice 91, 287, 296, 313, 367–368
 - divalent 122, 141, 151, 159, 192, 198, 204, 207
 - divalent lanthanide 149, 182
 - Eu^{2+} 366, 412
 - Fe^{5+} 92
 - fluorine 329–330, 385
 - heavy transition metal 99
 - isoelectronic 91, 149
 - isovalent 99, 152
 - Kramers 274, 331
 - lanthanide 4–6, 100, 146, 179, 182, 404, 406, 414
 - Mn^{4+} 3
 - multielectron 288
 - Ni^{2+} 3–4
 - Pr^{3+} 172
 - rare earth 1, 9, 43, 67, 99, 145–146, 209, 245, 287, 330, 349, 367, 389, 405, 409, 411–412, 423
 - tetravalent 118, 122, 141, 151–152, 164, 185, 204, 207
 - Ti^{3+} 295, 390, 401
 - Tm^{3+} 173–174
 - transition metal 3, 100–101, 277, 367, 385, 397
 - trivalent lanthanide 5, 149, 182, 411
 - vanadium 385, 397
- ions energy levels 309, 336–337
- irreducible representations
 - 265–268, 274–283, 293–294, 298, 325, 328, 333, 381, 398, 437
 - characters of 265–267, 269, 278
 - direct products of 278–279
 - one-dimensional 266, 276
- Jahn-Teller effect 383–385
- Jahn-Teller stabilization energy 383–385
- JJ-coupling 72
- Judd-Ofelt (JO) theory 405–406, 408
- lanthanides 4–5, 145–146, 164, 167, 171, 180, 185, 192–193, 195, 197–200, 203, 205, 208–209
 - divalent 201–202, 209
 - tetravalent 145, 167, 192, 197–198, 202–204, 207–209
 - trivalent 149, 182, 202, 209, 211, 213, 215, 217, 219, 221, 223, 225, 227, 229, 231, 233, 235, 237, 239, 404, 412
- Laplace's equation 49
- lasers 1, 3, 5, 41
- ligands
 - charged 295, 355
 - configurations 370
 - wave functions 308
- Lorentzian function 16
- Lorentzian profile 16–18
- LS-coupling 72
- LS terms 89–90, 93, 211–218, 222–240, 277, 298, 303, 318, 325
- free ion 326–327, 330

- impurity ion's 287
- luminescence 304, 362, 364
- magnetic dipole operator
 - 280–282, 406
- many-electron configurations 6
- multielectron configurations 80,
 - 93, 211, 310
- energy levels 396
- multielectron effects 390, 396
- nephelauxetic effects 91, 306–309
- non-radiative relaxation 173, 177,
 - 363, 367–368
- fast 41, 361–362
- nuclear charge, effective 201–202
- nuclear subsystems 351, 354, 367
- octahedral crystal field 293–294,
 - 299–302, 304, 307
- one-electron Hamiltonians 68
- optical materials 1
- orbital angular momentum
 - 62–63, 277
- orbital doublet 277
- orbital momentum 45, 71, 83, 94,
 - 148, 272–274, 277, 318
- orbital triplets 277–278, 310
- oscillator strengths 404–405, 407
- overlap integrals 312–313, 316,
 - 319, 321–322, 324, 334–335, 413
- parameterized calculations 183
- Pauli exclusion principle 67, 69,
 - 81–82, 95, 98, 304
- perturbation operator 21, 61,
 - 280, 290
- phonons 358–363, 369
- photons 3, 10–11, 14–15, 23
- physics, classical 45–46, 70, 73
- point symmetry 287, 309–311,
 - 412
- quantum mechanics 2, 14, 61–63,
 - 70–71, 73, 274
- quantum numbers 52–54, 58–59,
 - 65–69, 73–74, 76, 81–82, 86, 89, 94–95, 97, 148, 216–239, 272, 290–291, 312, 318
- magnetic 53, 65, 87, 290, 317,
 - 425, 429, 437
- orbital 59, 63, 65, 69, 73,
 - 81–82, 84, 98, 142, 164, 317
- principal 52–53, 65, 69, 81–82,
 - 95, 98, 142, 164
- Rabi oscillations 19, 21, 23, 25,
 - 27, 29
- Racah–Wigner algebra 148
- radiation 9–10, 12–14, 16–18,
 - 20–22, 24, 26, 28, 30, 32, 34–41
- absorption of 9, 30, 34, 37, 39
- electromagnetic 10, 38
- radiation frequency 13, 17, 35
- radiation intensity 34–35, 39
- radiative lifetimes 370, 405, 408
- radiative transition rates 407
- Rhys factor 357–360, 362, 365,
 - 369, 391
- Schrödinger equation 46–47, 49,
 - 51, 53, 55, 61, 67, 69, 274, 289, 349, 352, 354
- secular determinant 293, 374,
 - 377
- selection rules 57, 59, 279,
 - 281–282, 327, 329
- semi-empirical models 389–390,
 - 392, 394, 396, 398, 400, 402, 404, 406, 408, 410, 412, 414
- Slater integrals 87, 89, 91
- Slater parameters 101, 150, 152,
 - 159, 183, 185, 192, 198, 204, 207
- spectra
 - multielectron atoms 70

- trivalent lanthanide ions 182
- spin-doublet states 81, 278
- spin momentum 53, 63, 65–66, 79–81, 94, 272, 277
- spin-singlet states 81, 174, 304, 306, 327
- spin-triplet states 83, 327
- Stokes shift 364–367, 391, 394

- Tanabe–Sugano diagrams 298–299, 301, 303
- Ti³⁺ states 402–403
- transition metal ions salts 100
- transition probability, non-radiative 369
- transitions
 - absorption 9, 12, 14, 33, 39, 307, 358–362, 364, 405
 - absorption/emission 3, 10–11, 13, 366
 - Ce³⁺ 410
 - collision-induced 39
 - electric dipole 57, 59–60, 281, 358, 404–405
 - electronic 100, 146, 357, 404–405, 411
 - induced 11, 34, 41
 - magnetic dipole 282, 327–328, 405, 407
 - non-radiative 11, 367–371
 - radiative 41, 368, 370, 407–408
 - spin-allowed 86, 184, 303–304
 - spin-forbidden 86, 184, 303–304, 308–309
 - spontaneous 12, 43

- unit tensor operator 317–318, 405

- vibrational levels 354, 356, 358, 361–363, 368
- vibrational states 355, 367

- wave functions
 - electron 292, 351
 - hydrogen 54
 - one-electron 86–87, 317
 - radial 53, 142, 152, 164, 313
 - single-electron 272
 - two-electron 86
 - vibrational 358
- Wigner 3j-symbols 76–77
- Wigner 6j-symbols 328
- Wigner–Eckart theorem 317

- YAlO₃ 4, 335, 408
- YAlO₃ crystals 408
- YAM 410–411
- YAP, *see* yttrium aluminum perovskite
- yttrium aluminum perovskite (YAP) 335, 408–410, 413

- zero-phonon line (ZPL) 358–359, 364
- ZnAl₂S₄ 397–401
- ZPL, *see* zero-phonon line
- ZPL energy 361, 363, 366–367
- ZPL position 364–365, 367

“A great book covering the theoretical aspects of optical and luminescence properties of transition metals and lanthanides. Starting with the bachelor-level quantum physics to describe free transition metal and lanthanide ions, it covers the basics of crystal field theory, group theory, and the vibrating crystalline environment. The authors manage to keep the book at the graduate student level, making it accessible to the non-theorist and very well-suited for the interpretation and analysis of experimental data.”

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